

Alpha decay and identification of nuclides produced

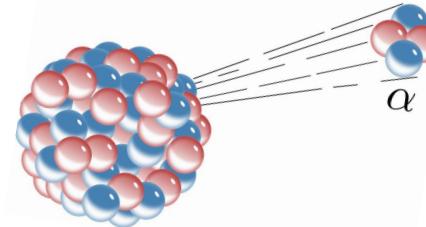
November 2023

Riccardo Orlandi

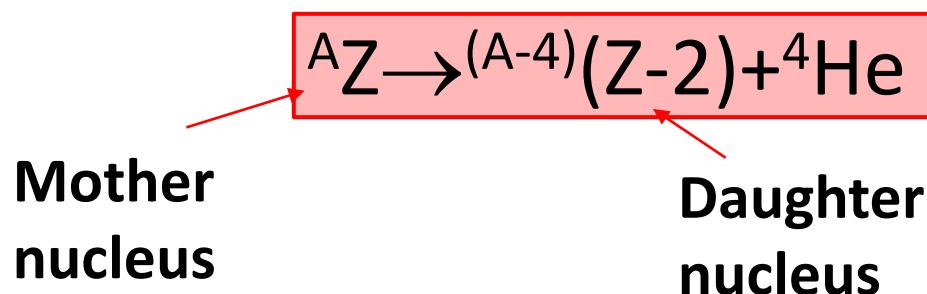
Outline

- Key Points of Alpha Decay
- Isotope Identification Examples

About Alpha Collapse



α Decay is a process by which an unstable nucleus gains stability by emitting an α particle, that is a nucleus of helium made of 2 protons and 2 neutrons



Alpha decay occurs spontaneously if the Q-value for the reaction is positive, i.e. $Q_\alpha > 0$.

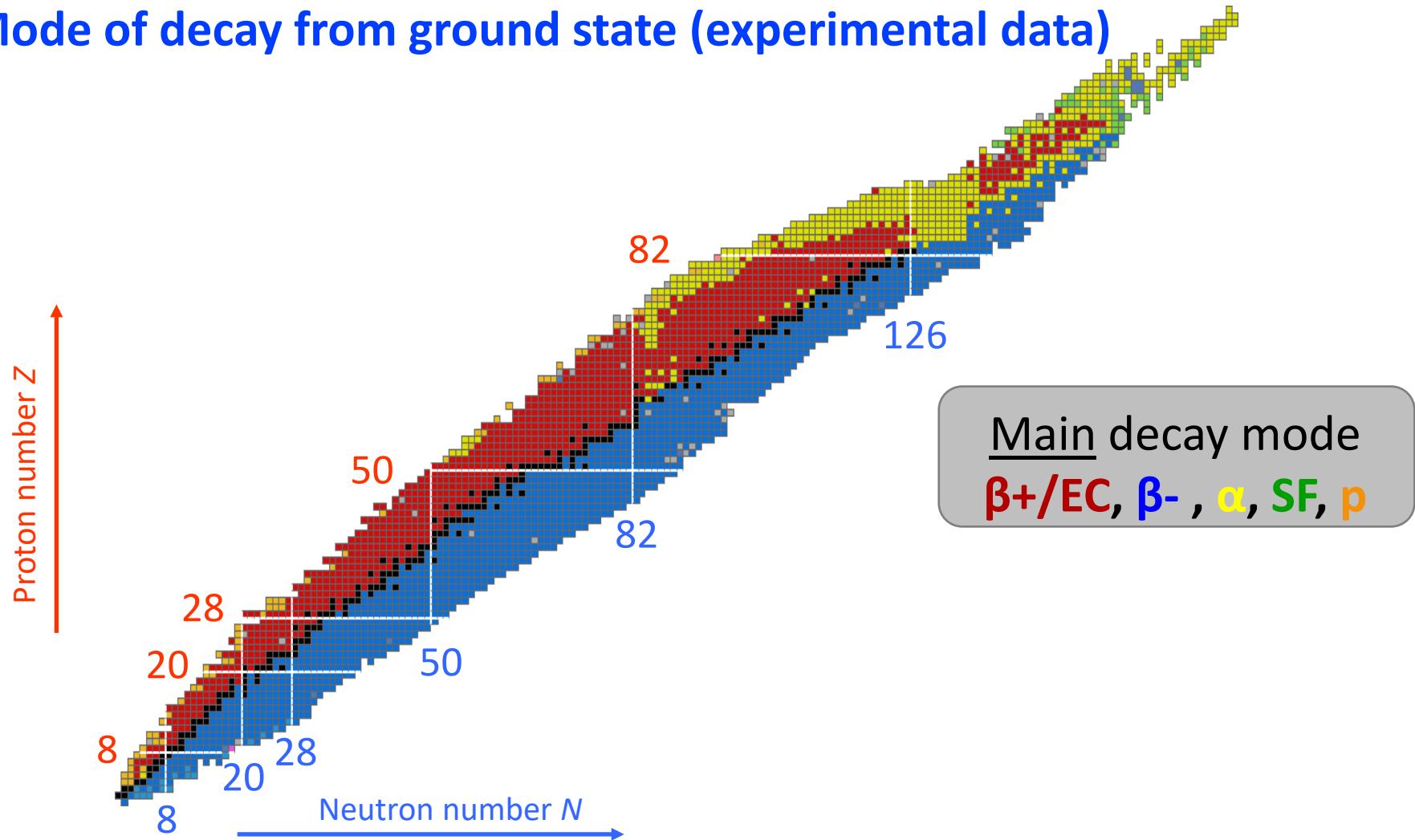
The Q-value is the difference of the mass of the mother (m_M) and the combined mass of the daughter (m_D) and α particle (m_α), multiplied by c^2 , i.e. :

$$Q_\alpha = m_M c^2 - (m_D c^2 + m_\alpha c^2)$$

In terms of the binding energies of the mother (B_M), daughter (B_D) and alpha (B_α)

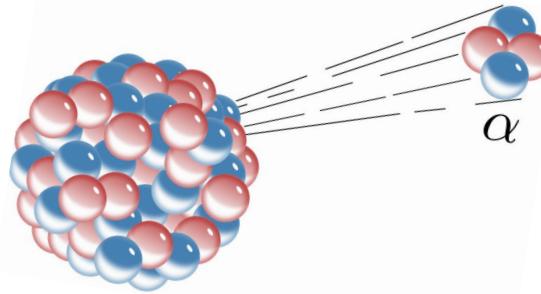
$$Q_\alpha = (B_D + B_\alpha) - B_M$$

Mode of decay from ground state (experimental data)



Alpha decay (yellow) in proton-rich, heavy nuclei

About Alpha Collapse



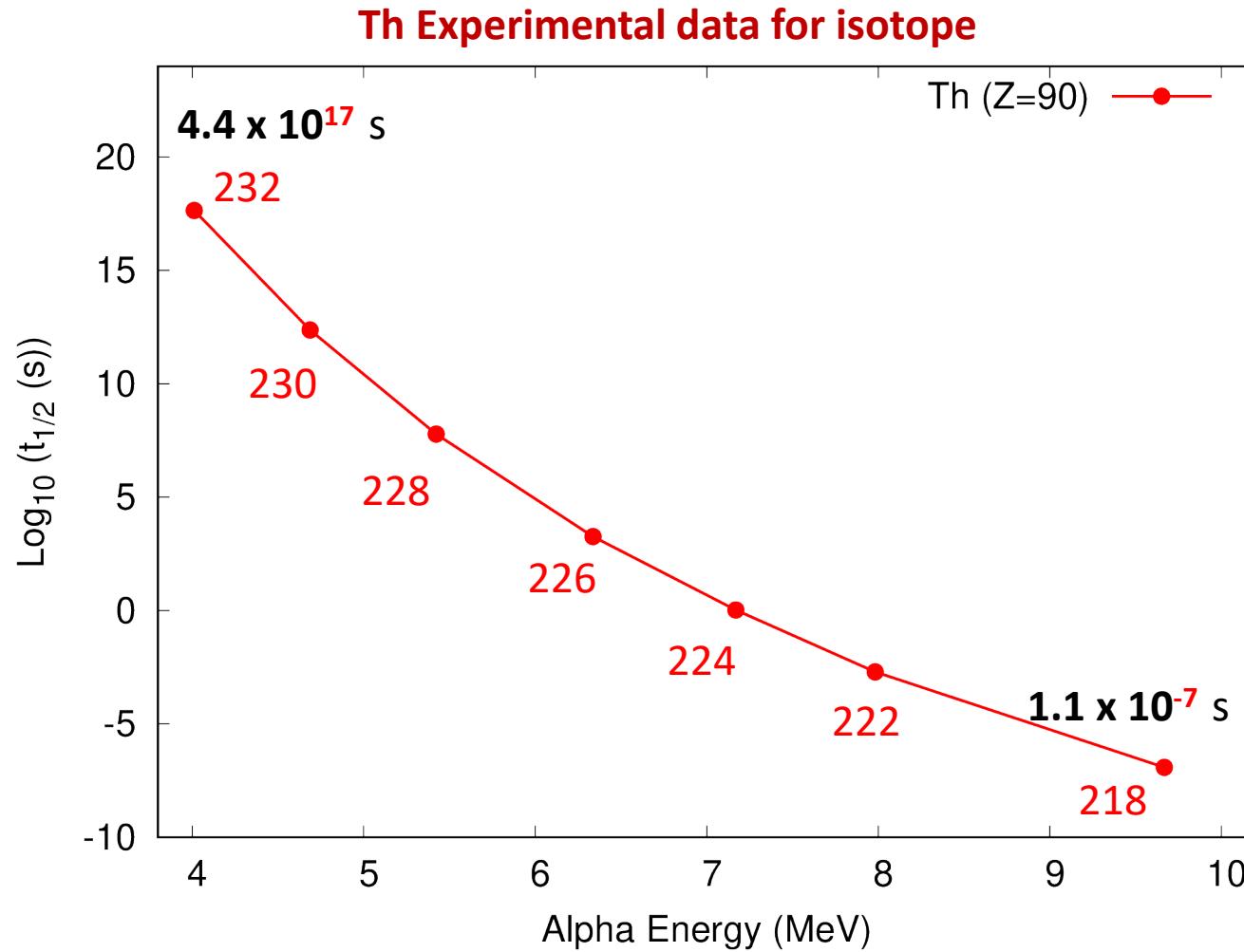
Experimental observables: E_α and $T_{1/2}$

Alpha energy can be derived from the law of conservation of momentum:

$$E_\alpha = \frac{m_D}{m_D + m_\alpha} Q_\alpha \approx \frac{A_D}{A_D + 4} Q_\alpha$$

Example $A=238$, $E_\alpha \approx 238/242$ $Q_\alpha = 0.983$ Q_α

About Alpha Collapse : Very large variation in half-life



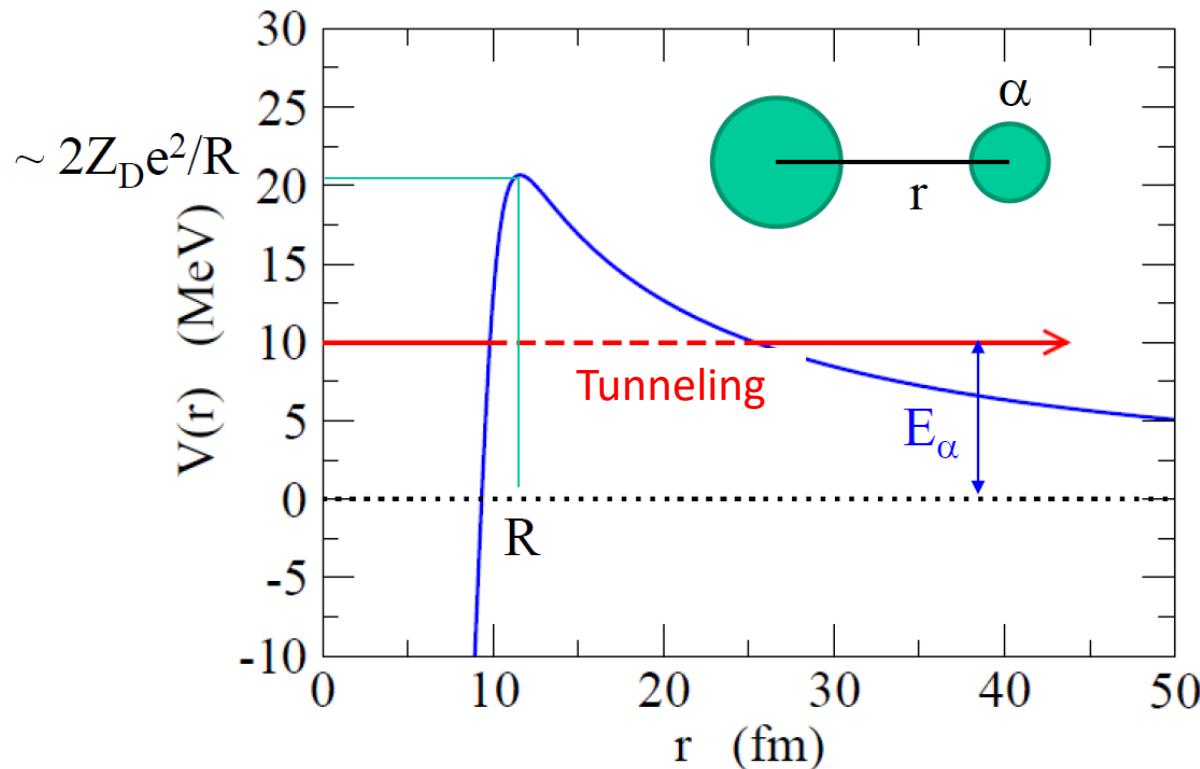
Even a slight change in E_α changes T_{1/2} by many orders of magnitude.

Example) ^{232}Th : $E_\alpha = 4.01 \text{ MeV}$, $T_{1/2} = 1.4 \times 10^{10} \text{ years} = 4.4 \times 10^{17} \text{ seconds}$

^{218}Th : $E_\alpha = 9.68 \text{ MeV}$, $T_{1/2} = 0.11 \mu\text{s} = 1.1 \times 10^{-7} \text{ seconds}$

Gamow's explanation of alpha decay

$E_\alpha < V_b \rightarrow$ Collapse due to tunnel effect



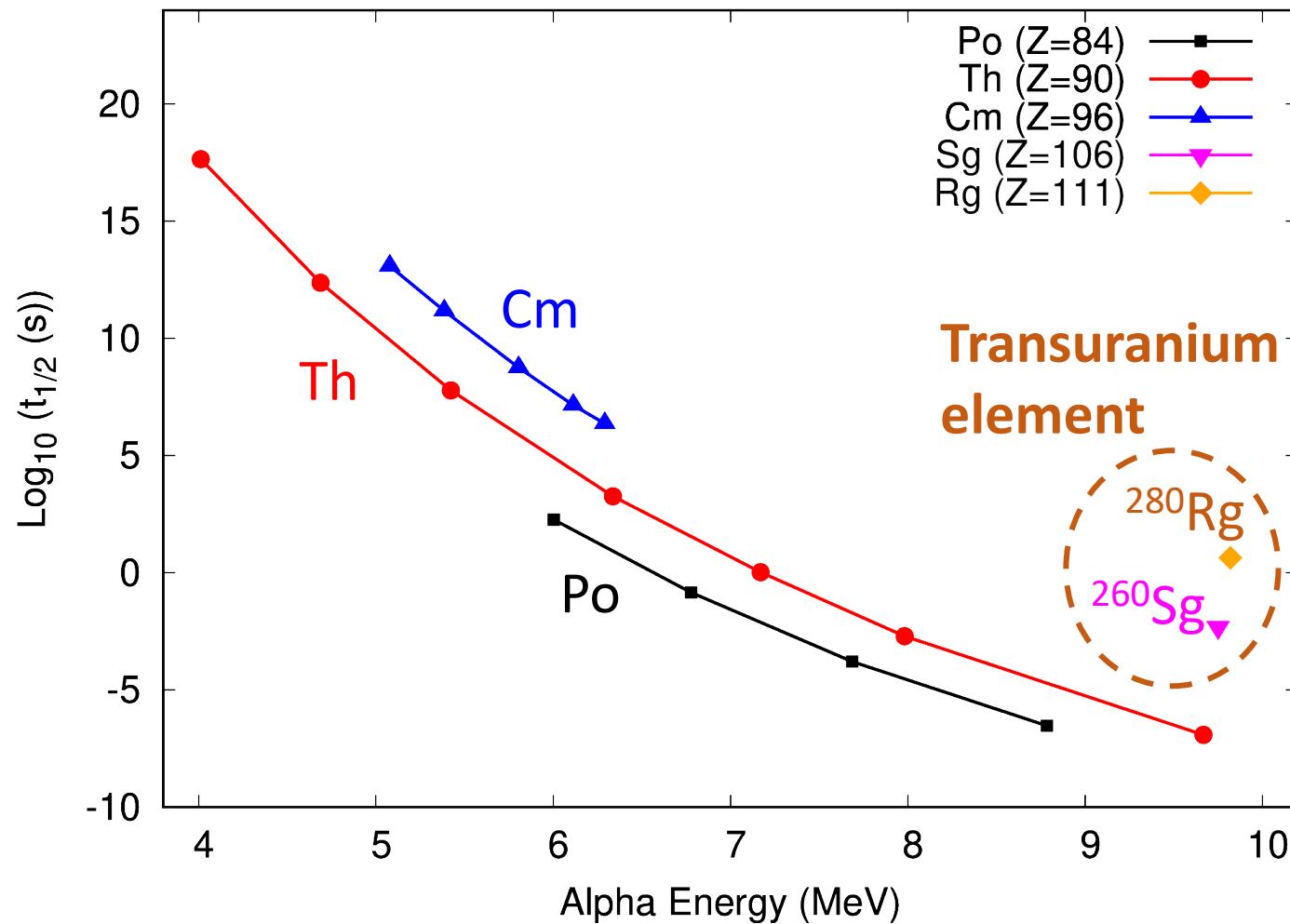
Example) Th Against isotopes

$$R \sim 1.2 \times (230^{1/3} + 4^{1/3}) = 9.26 \text{ fm}$$

$$V_b = \frac{q_1 q_2}{4\pi\epsilon_0 r} \cong 1.44 \frac{q_1 q_2}{r} = 1.44 \times \frac{88 \times 2}{9.26} = 27.3 \text{ MeV}$$

$E_\alpha(\text{Th}): 4 \sim 10 \text{ MeV} !$

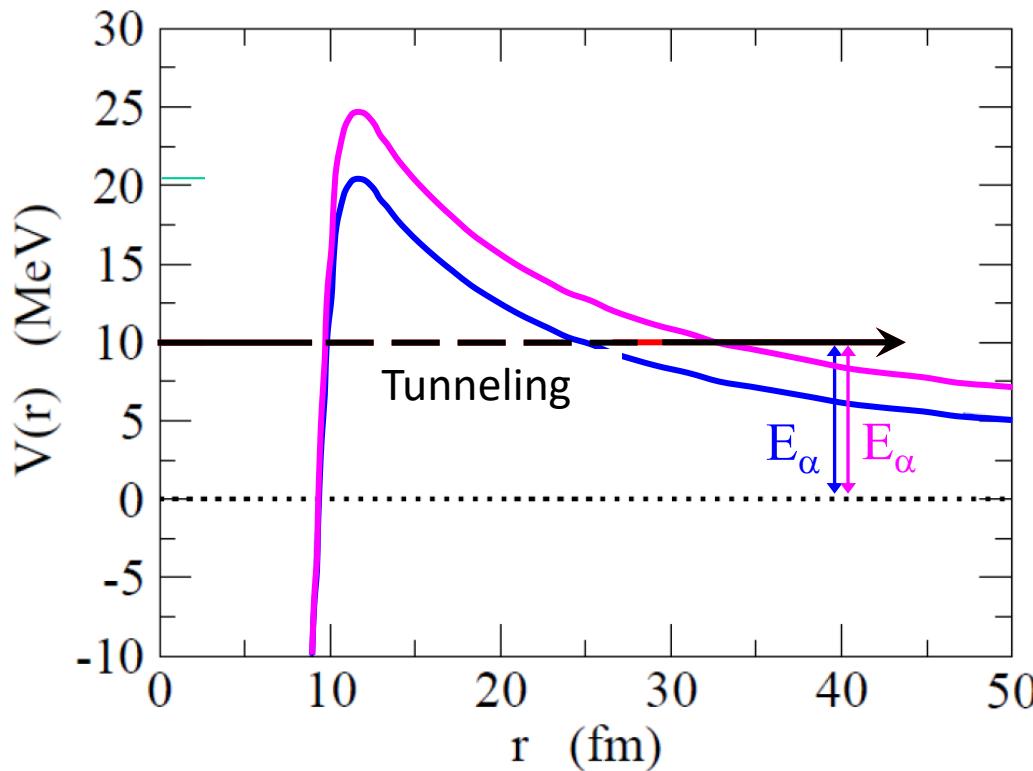
Relationship between half-life and element number



For the same energy, the alpha decay half-life increases with proton number
(Longer half-lives are one evidence of the formation of superheavy elements),
7

Gamow's explanation of alpha decay

$E_\alpha < V_b \rightarrow$ Collapse due to tunnel effect



The larger the atomic number, the larger the potential barrier.

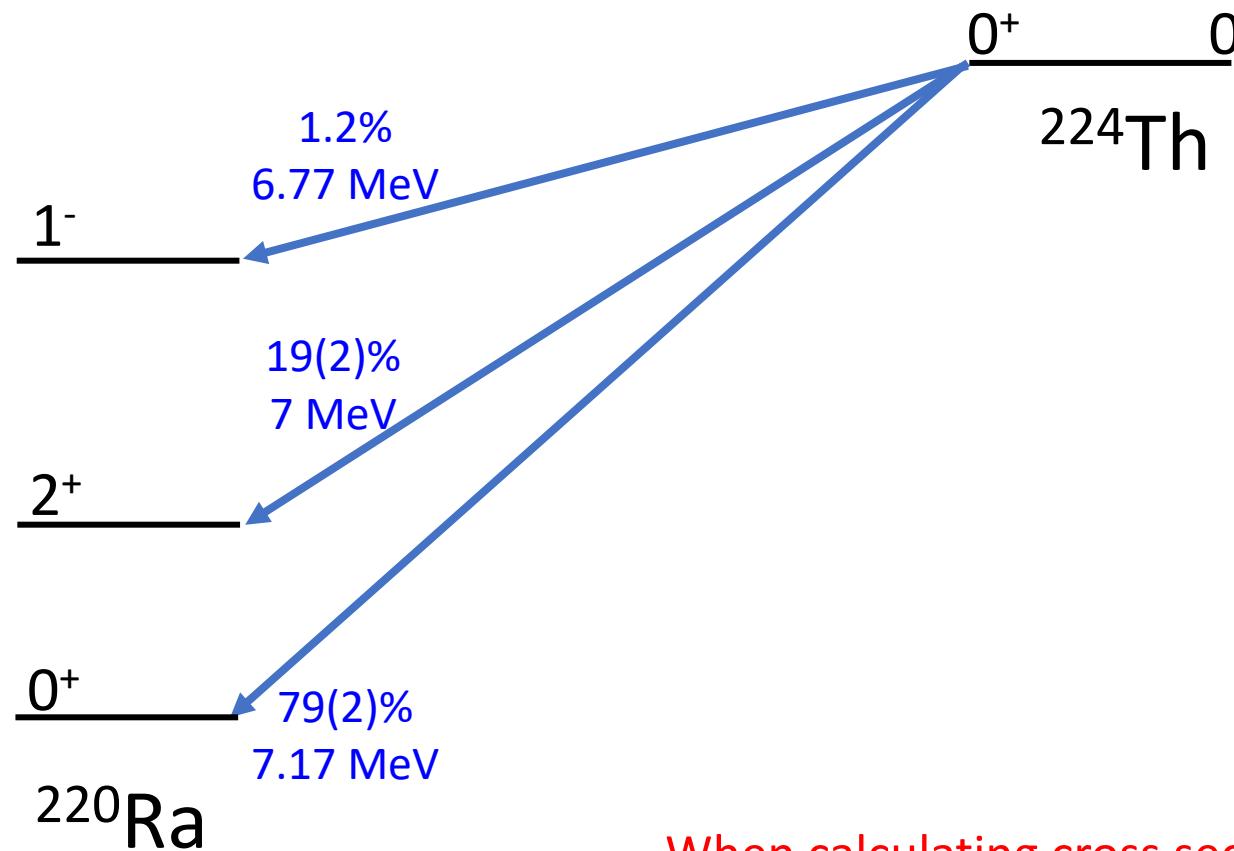
The same Q_α may also be due to the tunneling effect,

A slight increase in barrier height significantly increases the half-life

Branching of alpha decay

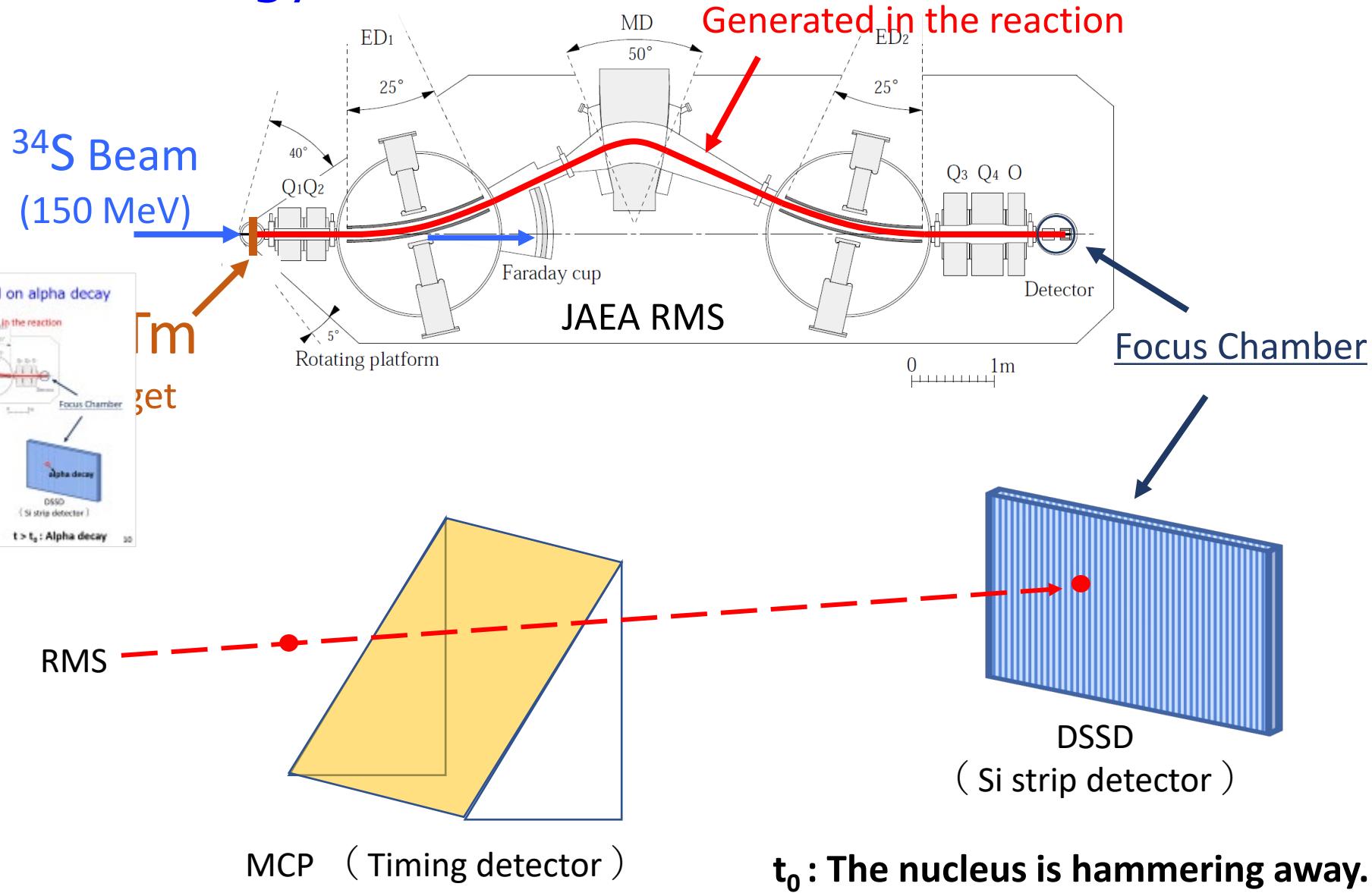
Some radionuclides undergo multiple forms of decay, called branched decay

例

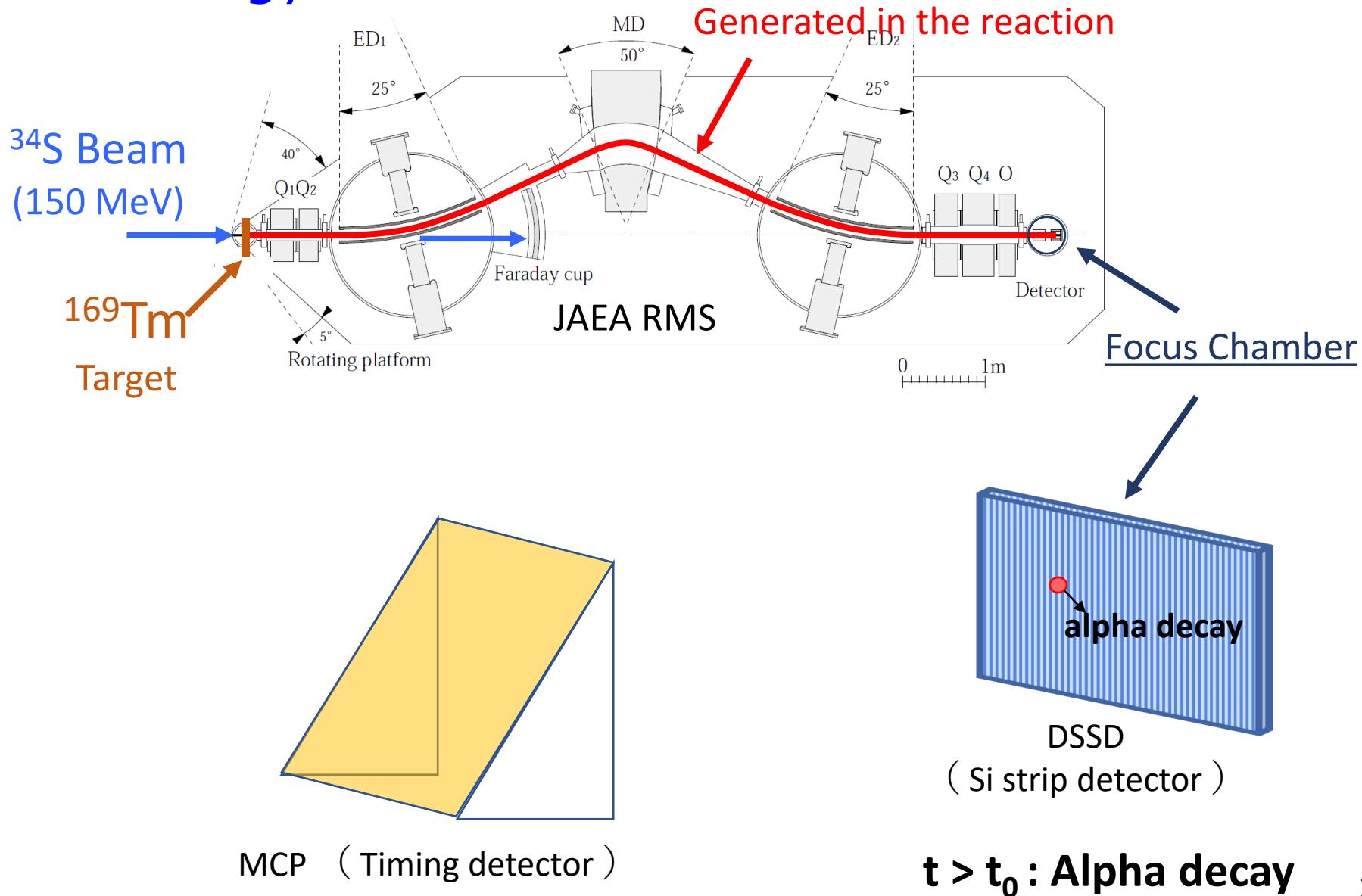


When calculating cross sections,
Branching must be taken into account

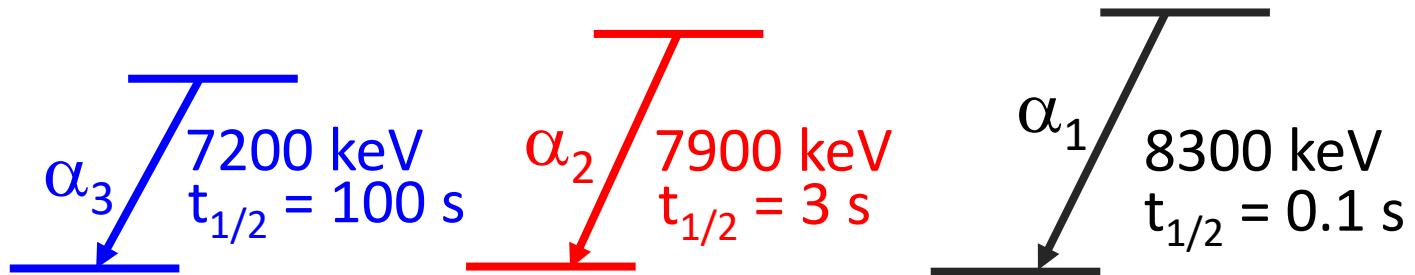
Nuclide identification based on alpha decay energy and half-life



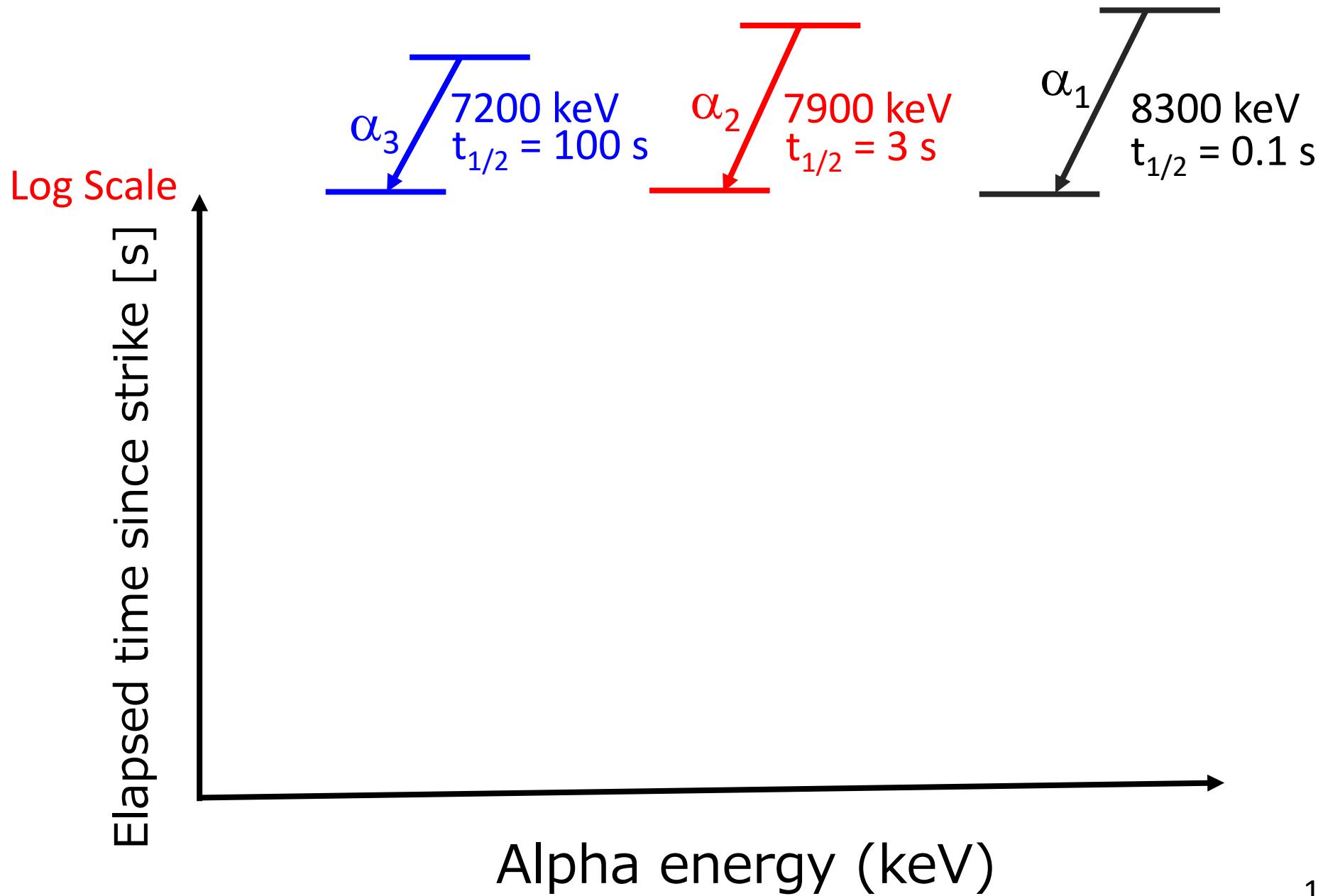
Nuclide identification based on alpha decay energy and half-life



Example

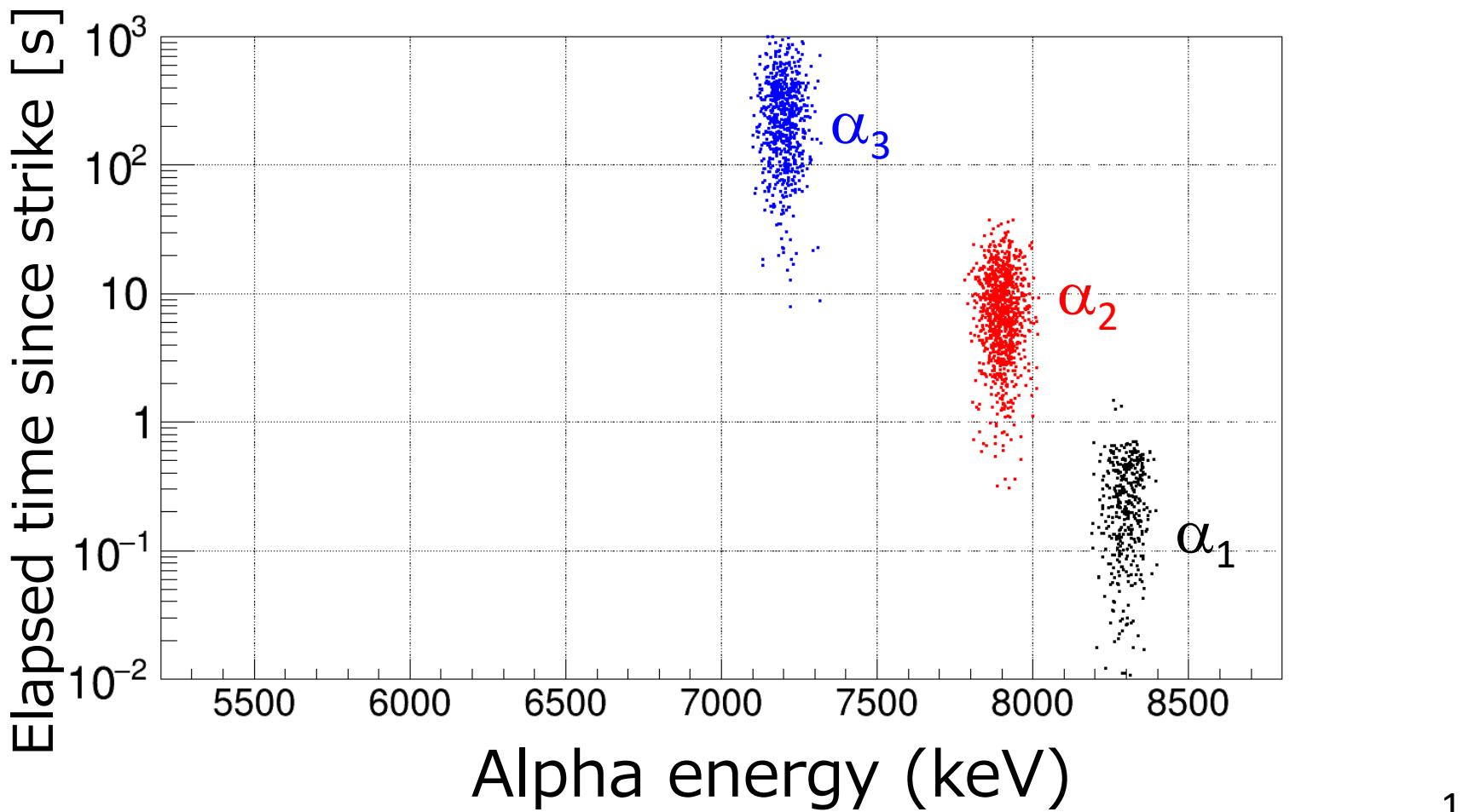


Example

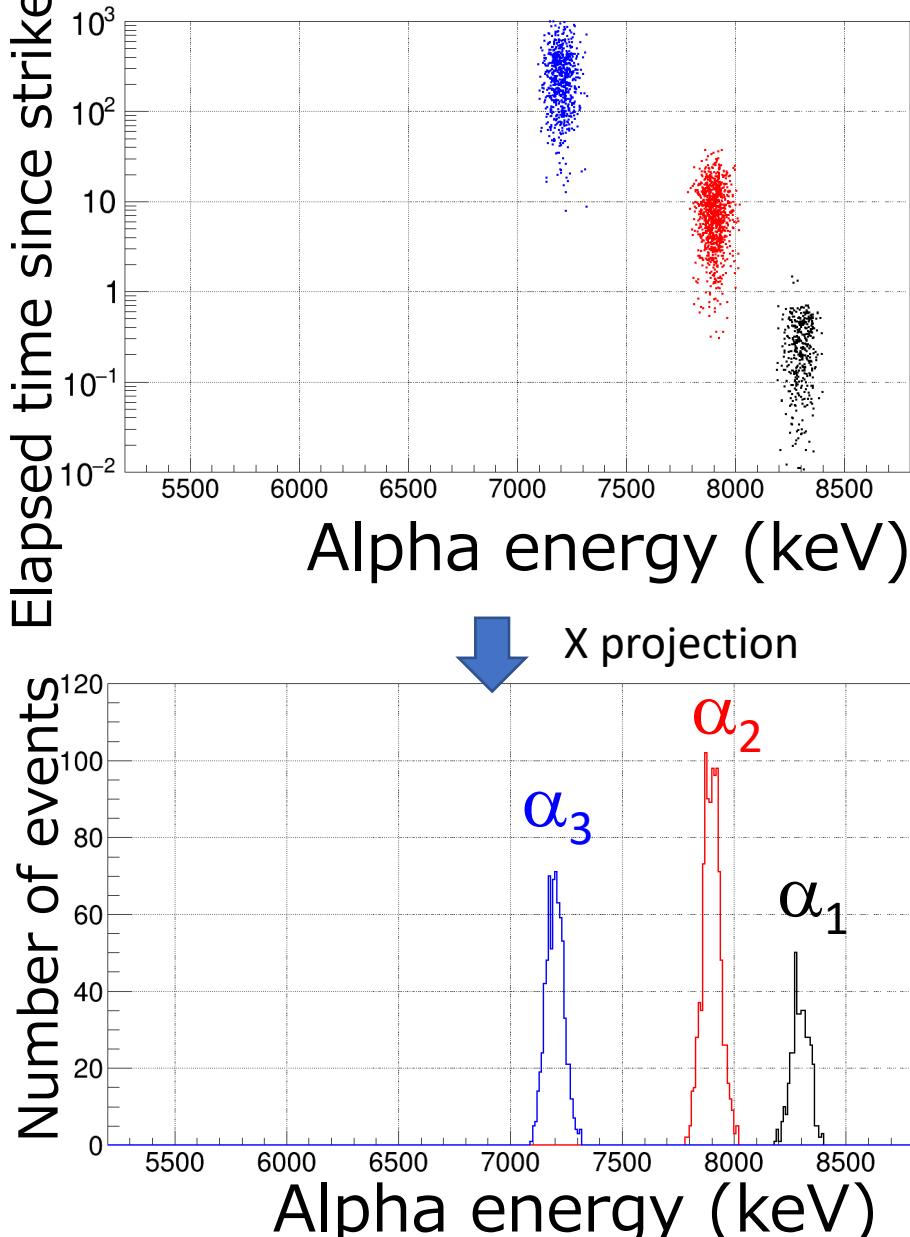


Example

Log Scale



Example

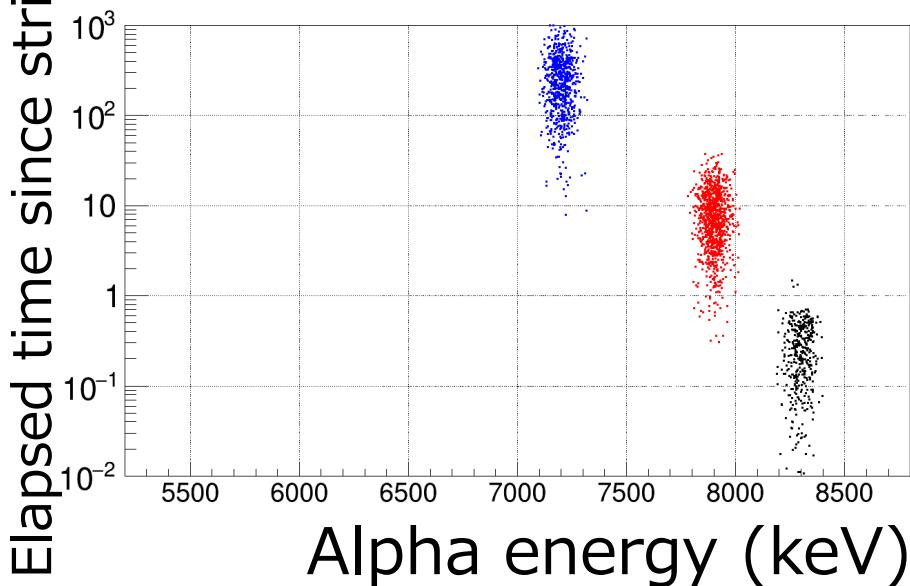


Alpha energy confirmed with database

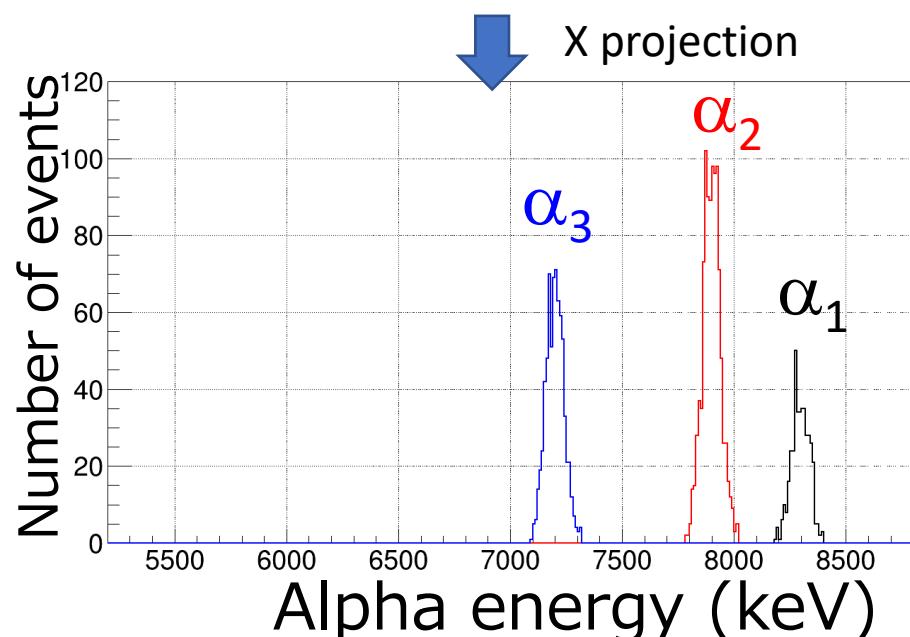
For example

National Nuclear Data Center (NNDC)
Radiation Search
https://www.nndc.bnl.gov/nudat3/indx_dec.jsp

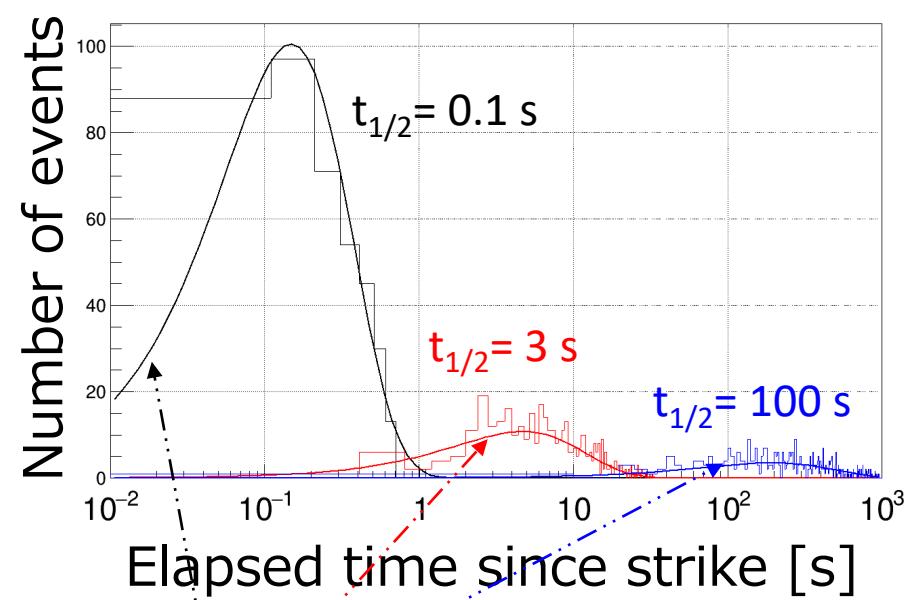
Example



Y proj



X projection



$$f = c * x * e^{-\frac{\ln 2}{b} x}$$

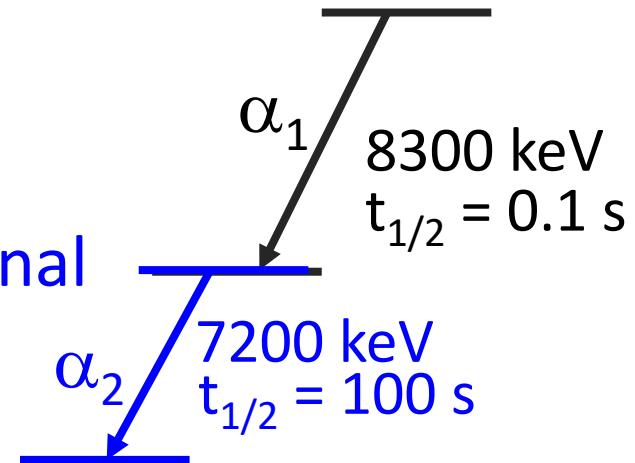
Parameter b is $t_{1/2}$
 x is Time

K.-H. Schmidt et.al.,
Z. Phys. A 316, 19-26(1984)

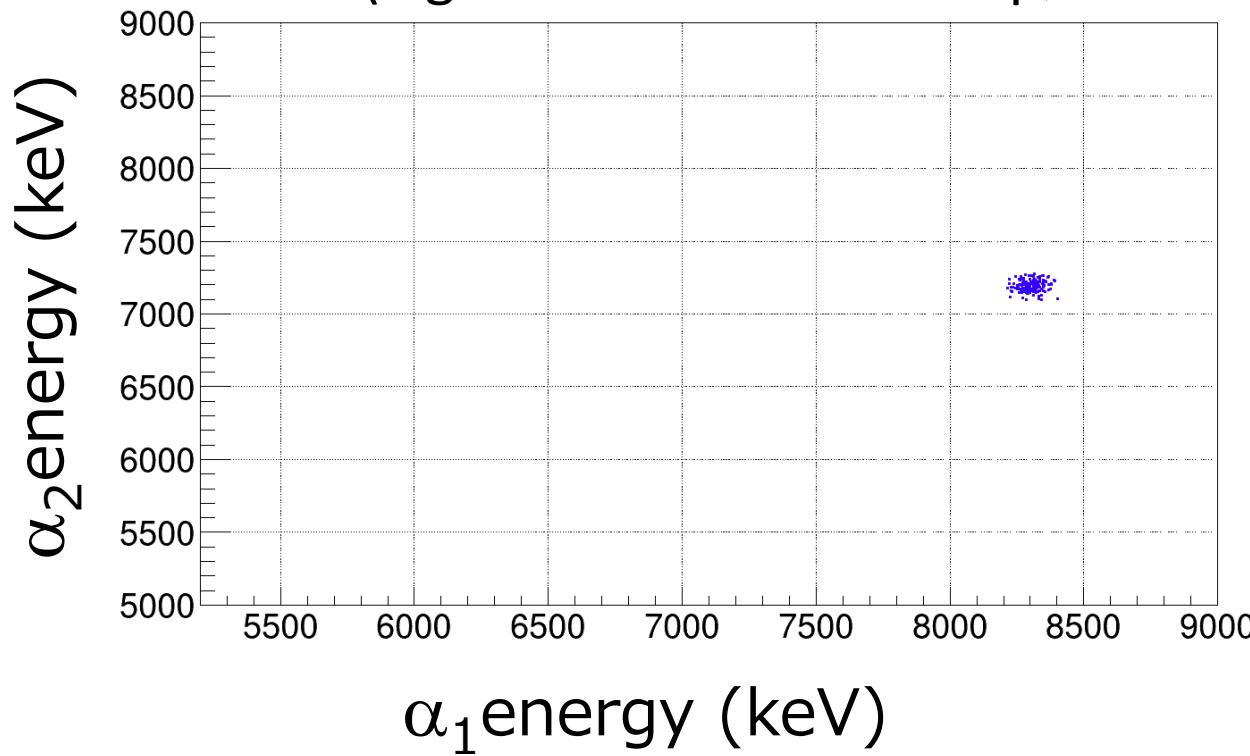
Example

For decay chains,

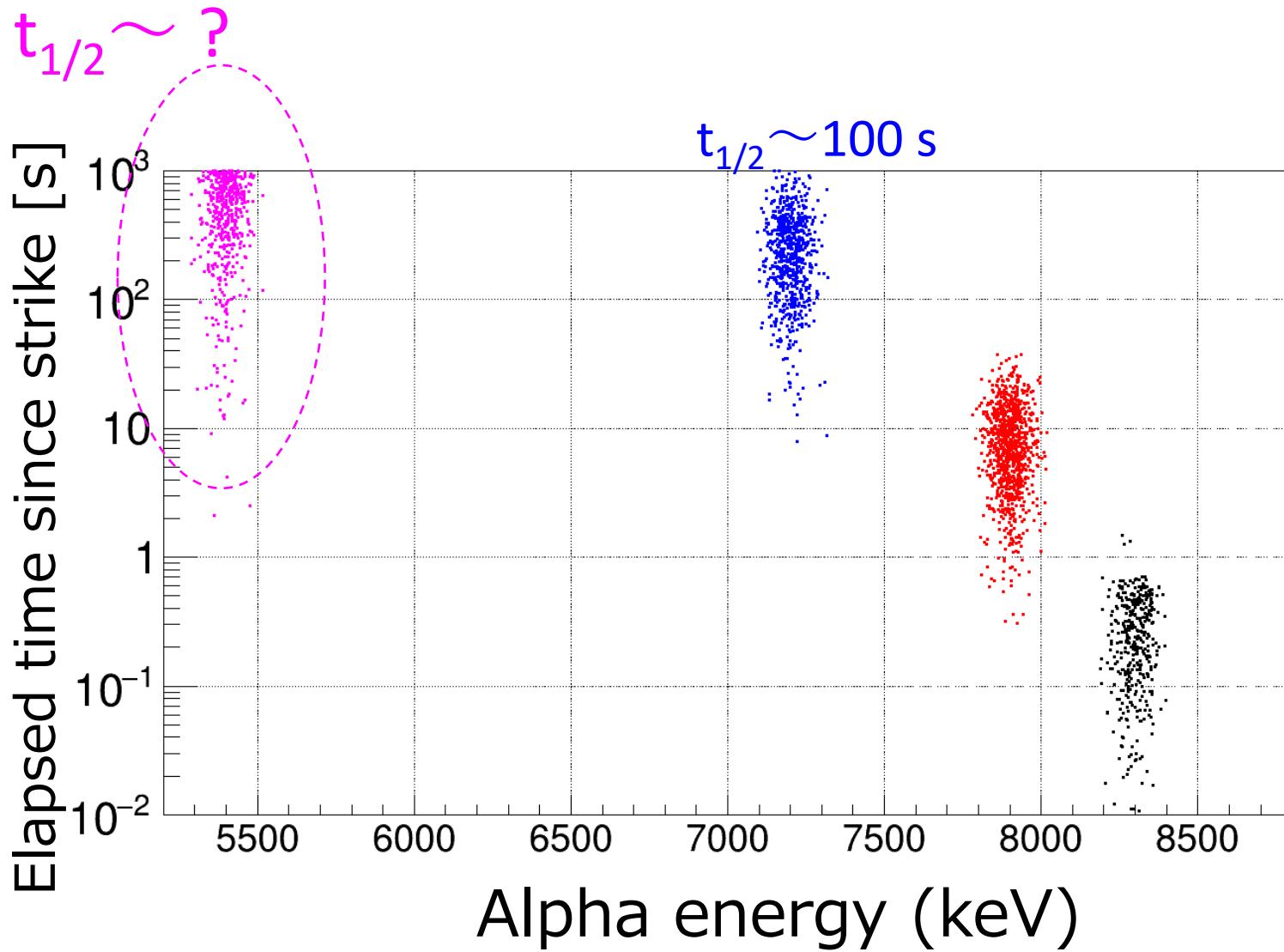
Correlated measurement of alpha signal



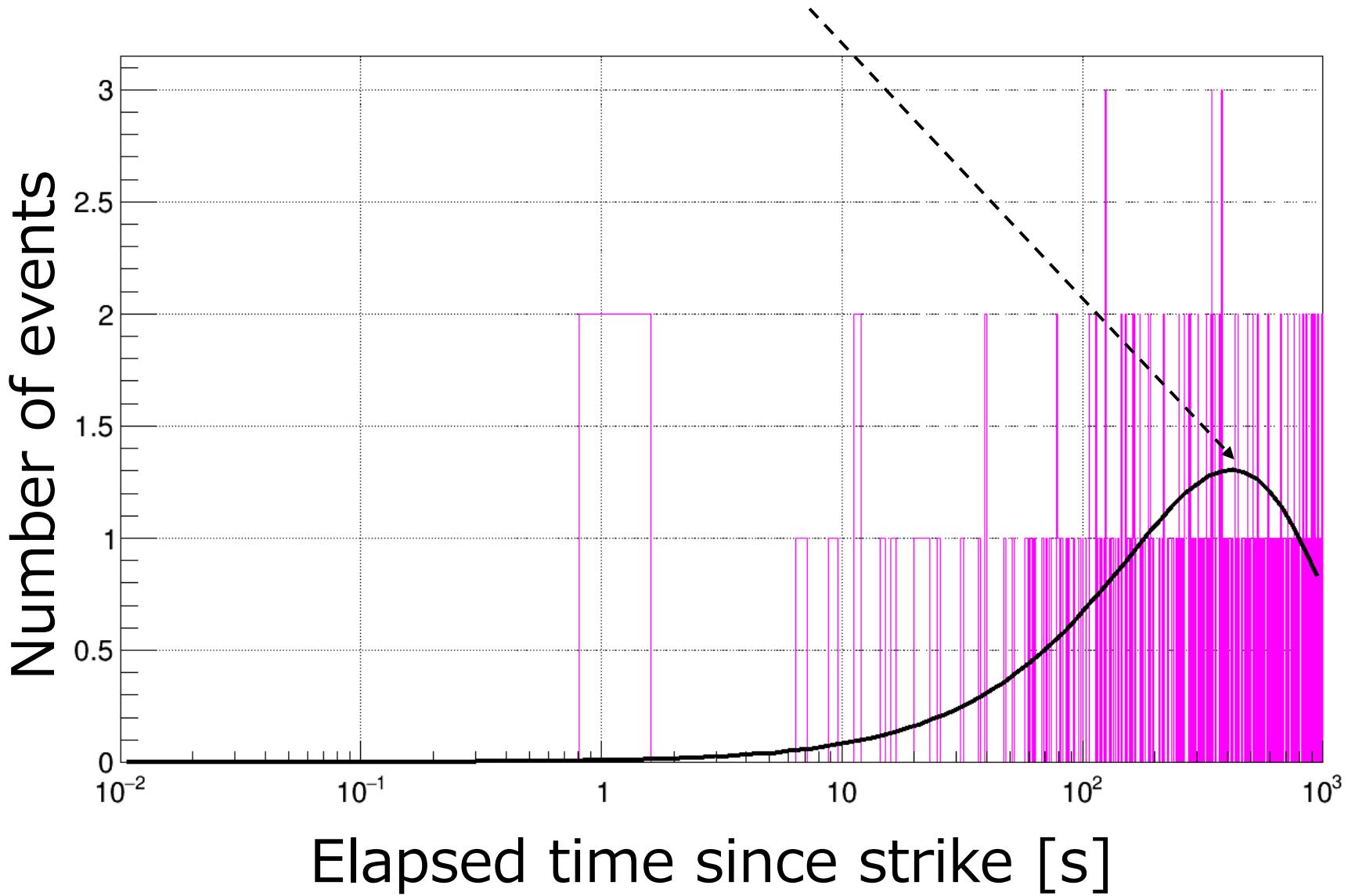
$\Delta t = t(\alpha_2) - t(\alpha_1) < \sim 300$ sec
(Figured on the same strip)



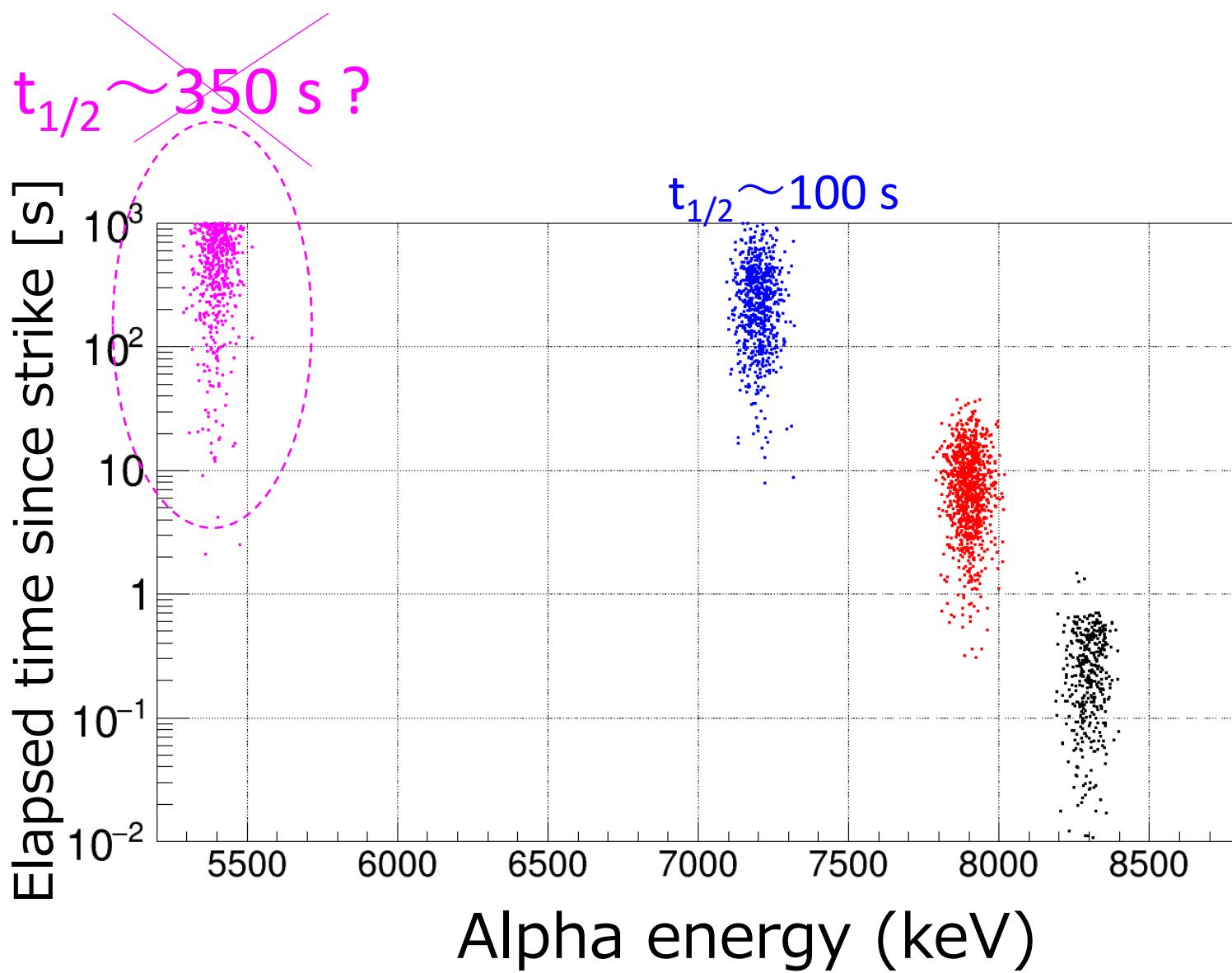
Example Important point



The $t_{1/2}$ appears to be ~ 350 sec, which is wrong, but ...



Example Important point



Actually constant **background**
(from nuclei with very long half-lives)

